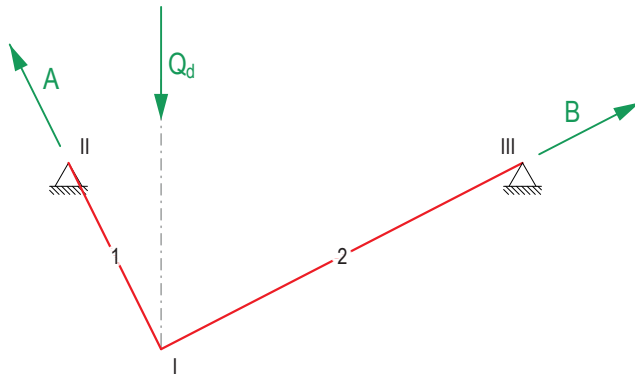


2.5

Dimensioning

Given is the form diagram of a cable made out of steel S235 under the live point load $Q_k = 30 \text{ kN}$. The required diameter of this cable is to be found.

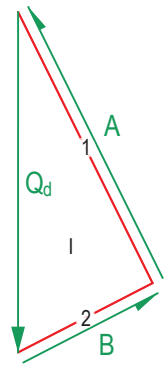
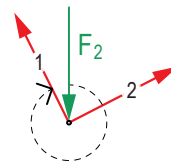
First the characteristic value (Q_k) of the acting force Q must be brought to the design level (Q_d). This is achieved by multiplying with the safety factor. Since the magnitude of a load over the lifetime of a structure cannot always be exactly predicted, a safety factor γ is calculated for each load. For dead loads the safety factor is $\gamma_G=1.35$ and for live loads $\gamma_Q=1.5$. With the found force Q_d the force diagram can be drawn.



$$Q_d = Q_k \cdot \gamma_Q$$

$$= 30 \text{ kN} \cdot 1.5$$

$$= \underline{45 \text{ kN}}$$



To calculate the cable diameter, the relevant force N_{dmax} in the structure is determined. The relevant force is understood to be the largest internal force. In this case, this is element 1 with a length of 4 cm, and therefore a magnitude of 40 kN.

$$N_1 = 40 \text{ kN} = N_{dmax}$$

$$N_2 = 20 \text{ kN}$$

$$A = 40 \text{ kN}$$

$$B = 20 \text{ kN}$$

If the relevant force N_{dmax} is divided by the material strength f_d , the required cross-sectional area A_{req} is obtained.

$$A_{req} = N_d / f_{td}$$

The strength of the given material can be taken from the formulary. Since 1 is a tensile element, the allowable tensile stress f_{tk} is relevant. A material safety factor γ_M is also included in the values of the material's strength to consider errors in the material. In contrast to the safety factor of the load, however, f_{tk} is divided by γ_M . γ_M is material-specific and can therefore also be taken from the formulary.

$$f_{td} = f_{tk} / \gamma_M$$

$$= 235 \text{ N/mm}^2 / 1.05 = 223.81 \text{ N/mm}^2$$

$$A_{req} = N_d / f_{td}$$

$$= 40 \text{ kN} / 223.81 \text{ N/mm}^2 = 178.7 \text{ mm}^2$$

Finally, the diameter is found using the formula for the circular area. Important: The result is always rounded up, as rounding off would result in a diameter smaller than the minimum requirement.

$$A = r^2 \cdot \pi = (D/2)^2 \cdot \pi$$

$$D = 2 \cdot \sqrt{A/\pi}$$

$$= 2 \cdot \sqrt{178.7 \text{ mm}^2 / \pi} = 15.08 \text{ mm} \approx \underline{16 \text{ mm}}$$

Stress proof

A cable cross-section of steel S355 with a diameter $D=20\text{mm}$ under a relevant tensile force $N_d = 80\text{kN}$ is given. The proof is sought whether the cross-section of the cable can withstand the given load.

$$N_d \leq N_{allow} = f_{td} \cdot A_{ef}$$

First, the maximum allowed force N_{allow} of the cable is to be found. This is calculated by multiplying the designed allowable tensile stress f_{td} with the effective cross-sectional area A_{ef} based on the given diameter of the cable.

$$A_{ef} = r^2 \cdot \pi = (D/2)^2 \cdot \pi$$

$$= (20 \text{ mm}/2)^2 \cdot \pi = 314.16 \text{ mm}^2$$

Second, the found force N_{allow} is then compared with the relevant force N_d . If N_{allow} is equal to or larger than N_d , the proof is provided and the given cross-section withstands the applied load. If the proof is not fulfilled, the cable must be re-dimensioned.

$$N_{allow} = f_{td} \cdot A_{ef}$$

$$N_{allow} = 338.1 \text{ N/mm}^2 \cdot 314.16 \text{ mm}^2 = \underline{106.2 \text{ kN}}$$

$$N_d = 80 \text{ kN} \qquad N_d \leq N_{allow} \quad \checkmark$$