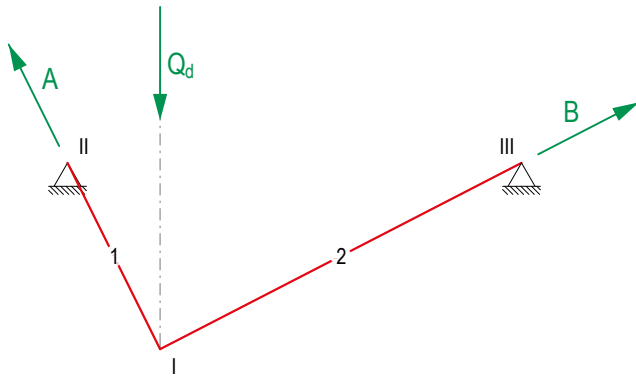


# 2.5

## Compendium Structural Design I & II Dimensioning

Given is the form diagram of a cable made out of steel S235 under the live point load  $Q_k = 30 \text{ kN}$ . The required diameter of this cable is to be found.

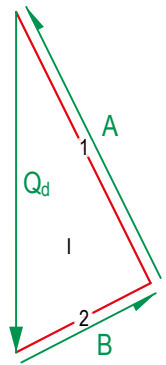
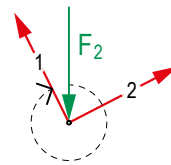
First the characteristic value ( $Q_k$ ) of the acting force  $Q$  must be brought to the design level ( $Q_d$ ). This is achieved by multiplying with the safety factor. Since the magnitude of a load over the lifetime of a structure cannot always be exactly predicted, a safety factor is calculated for each load. For dead loads the safety factor is  $\gamma_G=1.35$  and for live loads  $\gamma_Q=1.5$ . With the found force  $Q_d$  the force diagram can be drawn.



$$Q_d = Q_k \cdot \gamma_Q$$

$$= 30 \text{ kN} \cdot 1.5$$

$$= \underline{45 \text{ kN}}$$



To calculate the cable diameter, the relevant force  $N_{dmax}$  in the structure is determined. The relevant force is understood to be the largest internal force. In this case, this is element 1 with a length of 4 cm, and therefore a magnitude of 40 kN.

$$N_1 = 40 \text{ kN} = N_{dmax}$$

$$N_2 = 20 \text{ kN}$$

$$A = 40 \text{ kN}$$

$$B = 20 \text{ kN}$$

If the relevant force  $N_{dmax}$  is divided by the material strength  $f_d$ , the required cross-sectional area  $A_{req}$  is obtained.

$$A_{req} = N_d / f_{td}$$

The strength of the given material can be taken from the formulary. Since 1 is a tensile element, the allowable tensile stress  $f_{tk}$  is relevant. A material safety factor  $\gamma_M$  is also included in the values of the material's strength to consider errors in the material. In contrast to the safety factor of the load, however,  $f_{tk}$  is divided by  $\gamma_M$ .  $\gamma_M$  is material-specific and can therefore also be taken from the formulary.

$$f_{td} = f_{tk} / \gamma_M$$

$$= 235 \text{ N/mm}^2 / 1.05 = 223.81 \text{ N/mm}^2$$

$$A_{req} = N_d / f_{td}$$

$$= 40 \text{ kN} / 223.81 \text{ N/mm}^2 = 178.7 \text{ mm}^2$$

Finally, the diameter is found using the formula for the circular area. Important: The result is always rounded up, as rounding off would result in a diameter smaller than the minimum requirement.

$$A = r^2 \cdot \pi = (D/2)^2 \cdot \pi$$

$$D = 2 \cdot \sqrt{A/\pi}$$

$$= 2 \cdot \sqrt{178.7 \text{ mm}^2 / \pi} = 15.08 \text{ mm} \approx \underline{16 \text{ mm}}$$

### Stress proof

A cable cross-section of steel S355 with a diameter  $D=20\text{mm}$  under a relevant tensile force  $N_d = 80\text{kN}$  is given. The proof is sought whether the cross-section of the cable can withstand the given load.

$$N_d \leq N_{allow} = f_{td} \cdot A_{ef}$$

First, the maximum allowed force  $N_{allow}$  of the cable is to be found. This is calculated by multiplying the designed allowable tensile stress  $f_{td}$  with the effective cross-sectional area  $A_{ef}$  based on the given diameter of the cable.

$$A_{ef} = r^2 \cdot \pi = (D/2)^2 \cdot \pi$$

$$= (20 \text{ mm}/2)^2 \cdot \pi = 314.16 \text{ mm}^2$$

Second, the found force  $N_{allow}$  is then compared with the relevant force  $N_d$ . If  $N_{allow}$  is equal to or larger than  $N_d$ , the proof is provided and the given cross-section withstands the applied load. If the proof is not fulfilled, the cable must be re-dimensioned.

$$N_{allow} = f_{td} \cdot A_{ef}$$

$$N_{allow} = 338.1 \text{ N/mm}^2 \cdot 314.16 \text{ mm}^2 = \underline{106.2 \text{ kN}}$$

$$N_d = 80 \text{ kN}$$

$$N_d \leq N_{allow}$$